## Ch 3.2 Adding!

NOTE10: Flushing out binary addition in detail
Text reference: Section 3.2

Remember our 2's complement... binary addition means we can also do subtraction

Binary addition - 4 cases for adding two bits:

| A | 0 | 0 | 1 | 1 |
| :---: | :---: | :---: | :---: | :---: |
| $+\mathrm{B}$ | + 0 | + 1 | + 0 | + 1 |
| SUM | 0 | 1 | 1 | 0 <br> ~> carry the 1 |

Half adder - add two bits, truth table, SUM = XOR

| $\mathbf{A}$ | B | Sum | Carry |
| :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 0 |
| 1 | 0 | 1 | 0 |
| 1 | 1 | 0 | 1 |



Full adder - add two bits with carry-in, now 8 row truth table, 2 half adders and OR gate

| $\mathbf{A}$ | $\mathbf{B}$ | Carry <br> in | Sum | Carry <br> out |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 1 | 0 |
| 0 | 1 | 0 | 1 | 0 |
| 0 | 1 | 1 | 0 | 1 |
| 1 | 0 | 0 | 1 | 0 |
| 1 | 0 | 1 | 0 | 1 |
| 1 | 1 | 0 | 0 | 1 |
| 1 | 1 | 1 | 1 | 1 |



ALU from page 167 - this is a 1-bit slice of an ALU


Boolean and arithmetic operations, controlled by inputs F0, F1

| F1 | F0 | Operation |
| :---: | :---: | :---: |
| 0 | 0 | And $=A B$ |
| 0 | 1 | Or $=A+B$ |
| 1 | 0 | Invert $=B^{\prime}$ |
| 1 | 1 | Add $=A$ add $B$ |

Enables (ENA, ENB) and invert (INVA) operations happen first!
8 slices rippled together create an 8-bit ALU


